

Bandwidth Improvement of Dualband mm-wave Microstrip Antenna Using Genetic Algorithm

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Abstract: The necessity for multi-functional antennas with achievable performance from a single device is increasing dramatically. At the same, dual-band rectangular microstrip antennas are essential for a varieties of applications in mm-wave communication. This study aims to use a genetic algorithm to enhance the operating bandwidth of a dualband mm-wave microstrip antenna for wireless communication with binary-coded scheme. The patch surface was optimized by gridding it into 10X10 tiny rectangular blocks and designing them as non-conducting and conducting features to them. The proposed method has iteratively modeled the antenna using a Ansys HFSS and MATLAB to identify best fitted antenna. The optimized antenna has resonated at 39.1 GHz center frequency with 7.6 dB peak gain with 1.6 GHz bandwidth and at 50.2 GHz center frequency with 7.3 dB peak gain and 3.3 GHz bandwidth. The antenna's total efficiency is 71.4 % at 39.1 GHz and 92.8 % at 50.2 GHz.

Keywords: mm-wave antenna, dualband antenna, genetic algorithm , microstrip antenna

1. INTRODUCTION

The importance of wireless technology is growing rapidly in the sector. Specifically, mobile communication technologies have undergone significant changes before reaching the present 5G standard. A newly deployed 5G technologies will have a substantial effect in wireless communication. It is anticipated that it will provide high data rates and connect billions of users to the network [1]. This necessitates a wide bandwidth, which is available at the mm-wave frequency. Figure 1 depicts the estimated mm-wave spectrum available for wireless communication. This band, however, is sensitive to a number of difficulties, including significant propagation loss, obstruction, and atmospheric loss. Antenna optimization is critical for overcoming propagation problems and optimizing the available spectrum, bandwidth, directivity, and gain of mm-waves.

Especially, the investigation of multi-band antennas with relative effective qualities of bandwidth, efficiency, directivity and gain can meet the needs of communication. This form of antenna is required to provide a low profile, planar construction, and multi-band properties. Thus, patch antenna technologies are an appealing alternative because of their simple planar configuration, reduced size, cheap cost, ease of fabrication, and lightweight [3]. Nevertheless, typical microstrip antennas have limited bandwidth, low gain, and weak directivity [4], [5]. As a result, creating

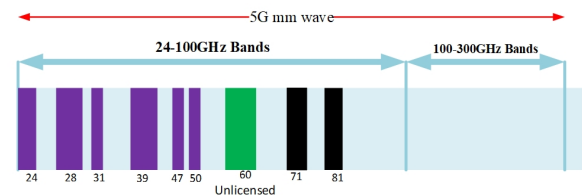


Figure 1. Predicted spectrum for mm-wave mobile communication [2]

multi-band microstrip patch antennas is always a challenging problem.

Several methods for enhancing patch antennas with dualband operation have been documented in the literature. In dual band antenna were designed in various mechanisms among them based on artificial magnetic conductor [6], and C and O slot structure [7] were presented. U-shaped slot dualband patch antenna resonates at 28GHz and 38GHz is described [8]. A dualband elliptically slotted circular radiating patch with resonant frequencies of 28 and 45 GHz is proposed [9]. Dual-band antenna also designed using branch fractal bionic antenna as described in [10]. In [11], the authors introduced a dualband single antenna by a band switching mechanism

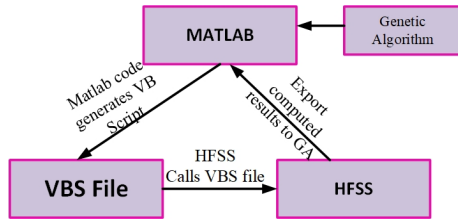


Figure 2. Combination of MATLAB and HFSS in optimization procedure for single execution

that resonates at 27.5 GHz and 39GHz. For dualband operation at 28 GHz and 38 GHz, a slot patch antenna was presented [12]. Dualband antenna also modeled using varieties of autonomous algorithm such as auto-context system learning [13], Gaussian’s deep learning process [14], as well as evolutionary algorithms like genetic [15]. In [16], a dualband optimization of a patch antenna in microwave frequency using a genetic algorithm is described. The author of [17] describes a dualband antenna using genetic algorithm at mm-wave with a circular cell.

This study uses a binary-coded genetic algorithm to enhance the impedance bandwidth of a dualband microstrip antenna for mm-wave mobile applications. The procedure is carried out on the patch surface to produce a new geometry by altering the gridded rectangular blocks. The combination of MATLAB and HFSS was utilized to simulate and model the antenna. HFSS employed to model, compute and exporting the results of parameters to MATLAB’s main function [18]. The optimized antenna’s revealed performances are transferred to the algorithm for additional fitness computation, and the algorithm performs parent selection for continuous generation. As shown in Figure 2, the optimizer code is written in MATLAB, and HFSS receives the details of the antenna from the VBS file generated by MATLAB.

2. ANTENNA MODELING

The proposed antenna was first modeled to have a rectangular radiating patch on a 10×10mm² Roger substrate. The substrate has a 2.2 dielectric strength, 0.5 mm thick and very low tangent-loss approximately 0.009. The starting dimension of a reference model, rectangular microstrip antenna, was determined using the fundamental method provided in [19]. The anticipated dimensions, however, do not provide appropriate performance at the desired center frequencies and bands. Thus, para-metrics analysis was applied to determine the actual length and width of the patch. When the resonance frequency is desired at 39 GHz, the optimal patch length was 5.6 mm and the width was 6.6 mm. A 50 Ω microstrip feed line having 2.6mm length and 0.75mm width is connected to the patch. Figure 3 presents the dimension of reference model, which is ready for patch geometry optimization.

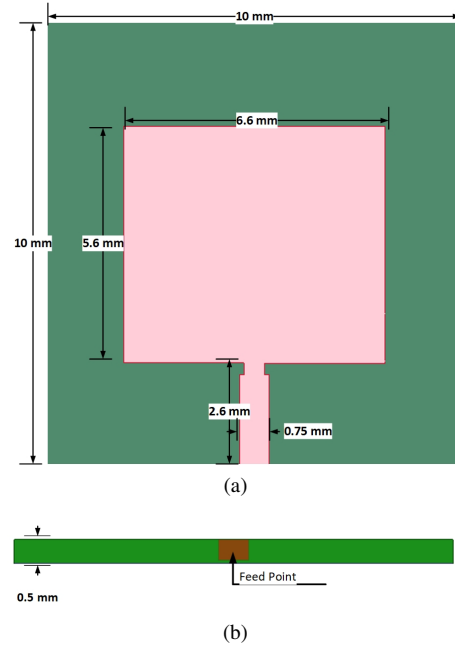


Figure 3. (a) Reference model designed to operate at 39.0GHz (b) side view.

3. GENETIC ALGORITHM PROCEDURE

In genetic algorithm(GA) optimization, the next offspring is reproduced from best fitted chromosomes, which mimics the procedure of natural selection [20]. In GA, each individual is symbolized by chromosomal or a sequence of bits [21]. The algorithm starts from random generation and reproduces the next generations iteratively until the halting criteria is reached. [22]. The flowchart diagram of a genetic algorithm is presented in Figure 4.

Figure 5 illustrates the segmentation of patch surface into 10 × 10 tiny random rectangular blocks, which is suitable for optimization. The cell’s properties may be simply specified as non-conducting and conducting using a binary-coded approach. Boolean "1" is given to the corresponding gene if the cell is conducting, whereas a binary "0" is attributed to a non-conducting genes. [23]. The goal of this optimization is to look into improving the operating bandwidth with dual-band resonance. As a consequence, the objective functions is built as follows:

$$FitnessFunction = \frac{-1}{N} \sum_{i=1}^N (Bw - S_{11}(f_{ii})) \tag{1}$$

$$Bw = Bw_1 + Bw_2 \tag{2}$$

where

$$Bw_2 = f_{H2} - f_{L2} \tag{3}$$

$$Bw_1 = f_{H1} - f_{L1} \tag{4}$$

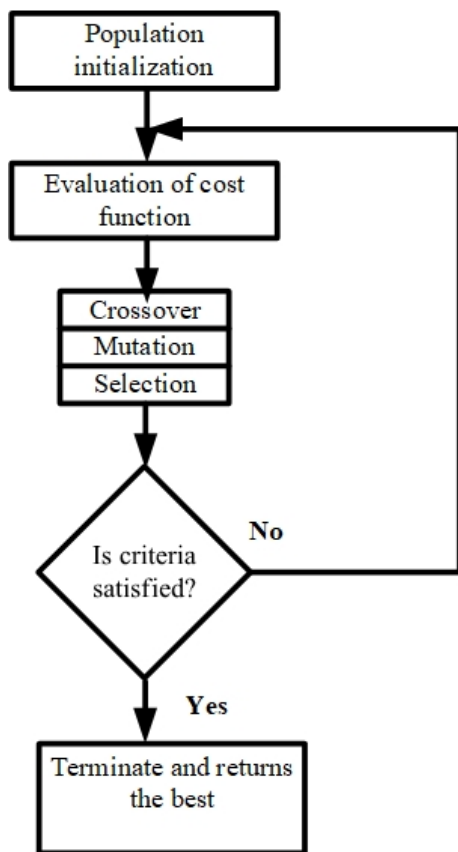


Figure 4. Flowchart of genetic algorithm

$$Bw = \begin{cases} 5GHz & \text{if } Bw \geq 5GHz \\ Bw & \text{if } Bw \leq 5GHz \end{cases}$$

Where $S_{11}(f_{ii})$ is designed as.

$$S_{11}(f_{ii}) = \begin{cases} S_{11}(f_{ii}) & \text{if } S_{11}(f_{ii}) \geq -10dB \\ -10dB & \text{if } S_{11}(f_{ii}) \leq -10dB \end{cases}$$

where

f_{ii} : sampling frequency in the interval of 100 MHz

$S_{11}(f_{ii})$: reflection coefficient in dB

Bw : total operating bandwidth of antenna

Bw_1 : bandwidth of antenna at the first operating band

Bw_2 : bandwidth of antenna at the second operating band

f_{H1} :higher operating frequency in a first band

f_{H2} :higher operating frequency in a second band

f_{L1} :Lower operating frequency in a first band

f_{L2} :higher operating frequency in a second band

N : Number of sampling frequencies in a given band

The genetic algorithm optimization setup has been arranged and summarized in Table I.

The solution-space has a total of $2^{100} = 1.3 \times 10^{30}$ individuals. If each individual computational time is 1 second, the total computing required to identify the best-fitted individual will be 1.2×10^{24} years. However, owing to the algorithm, the fitted one was selected about 44.86 hours by a RAM of 8GB and 2.7 GHz processor computer. The

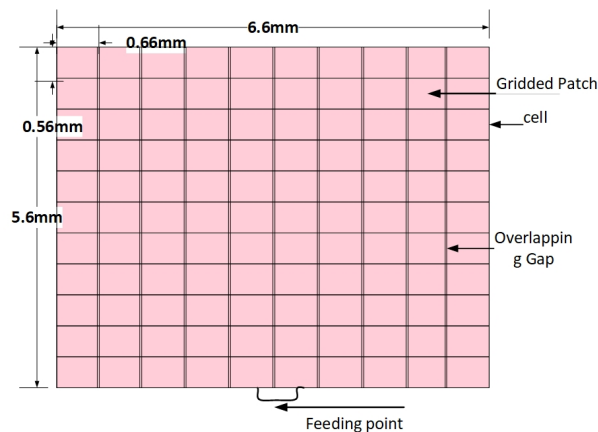


Figure 5. Distribution of 100 rectangular blocks on reference patch surface

TABLE I. Optimization setup for genetic algorithms

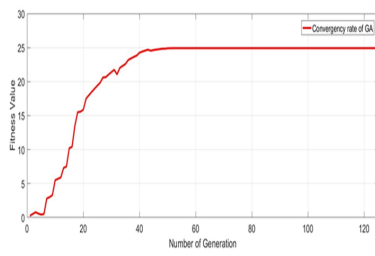
No.	Parameters	Set up figures
1	Clustered population	30
2	No. of Cells	100
3	No. of generation	125
4	Crossover	Single-point
5	Crossover Probability	0.7
6	Mutation	Single-bit
7	Mutation-rate	0.02
8	Kind of Selection	Tournament

iteration were conducted for 125 generations and started to converge after 48 iterations as illustrated in 6(a). The final optimized geometry is presented in Figure 6(6).

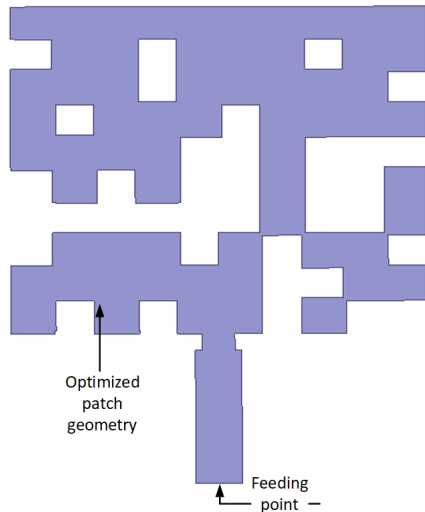
4. RESULTS AND DISCUSSION

ANSYS HFSS was used to simulate the reference and the genetic modified antennas. The baseline antenna operates in a single band and has a covering impedance bandwidth of 1.2 GHz at 39 GHz. The reference model's peak S_{11} value at 39 GHz is -17.6 dB, where the antenna's greatest actual gain is 5.4 dB. The suggested genetically engineered antenna, nevertheless, operates at two separate frequencies: 39.1 GHz and 50.2 GHz. The frequent slots produced by the algorithm aid in the patch surface's ability to remove uncorrelated current distribution, which improves the antenna's radiation characteristics. The slots also lengthen the current flow on the area of radiating patch, which facilitating the antenna's capability to operate at dualband frequencies.

The results revealed that the bandwidth of the antenna has improved in both frequency spectrum. The directivity and gain of the antenna are also acceptable for mm-wave cellular systems. The antenna resonates at 39.1 GHz and 50.2 GHz, as shown in Figure 7, with the return loss values of $S_{11} = -12.6$ dB and $S_{11} = -26.0$ dB, respectively. With the engineered antenna, there was a noticeable increment in overall bandwidth when $S_{11} \leq -10$ dB was considered.



(a)



(b)

Figure 6. a) average fitness-value vs number of generation, b) Fittest patch geometry

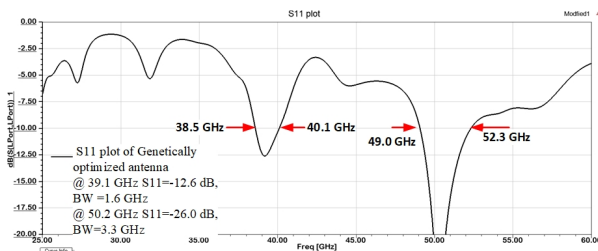


Figure 7. S_{11} result for the engineered antenna

At 39.1 GHz, it has achieved 1.6GHz or 4.1% bandwidth. A 3.3GHz or 6.6 % bandwidth was also attained at 50.2GHz frequency with the improved antenna. This increased bandwidth capabilities are crucial for mobile broadband services. VSWR is less than 2 in both operational bands (38.5 GHz – 40.1 GHz) and (49.0 GHz – 52.3 GHz).

Furthermore, directivity enhancement in both working bands was seen in Figure 8. At 39.1 GHz, broadside direction peak directivity was 7.9 dB, while at 50.2 GHz, directivity was 7.4 dB.

At two operational frequencies, the 3D antenna's gain plot is shown in Figure 9. At 39.1 GHz, the max gain

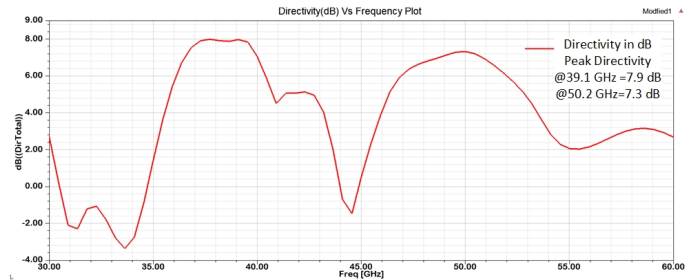
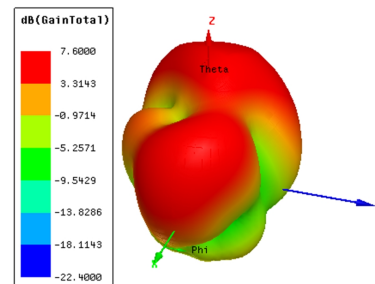
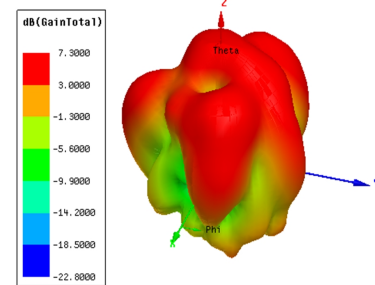


Figure 8. Directivity versus frequency plot of genetically optimized antenna $\phi=90^{\circ}$ and $\theta=0^{\circ}$



(a)



(b)

Figure 9. The 3D gain plot of engineered antenna (a) 39.1 GHz (b) 50.2 GHz.

of optimized antenna is 7.6 dB. And at 50.2 GHz the peak gain of antenna was resulted approximately 7.3 dB. In Figure 10, the radiation pattern of optimized antenna was presented and it shows that radiation pattern was directed in a broadside orientation. The antenna has an overall efficiency of 89.3% at 39.1 GHz and 98.8% at 50.2 GHz as presented in Figure 11.

The distribution of current on the radiating surface of the engineered antenna is displayed in Figure 12 at 39.1 GHz and 50.2 GHz resonance bands. On the edges of cells and around the junction points between the feed line and the optimized patch, a greater degree of current dispersion is visible.

As indicated in Table II, the antenna performance parameter was compared to several relevant works. The double bow-tie approach in [24] had a comparable bandwidth with this result. The antenna's bandwidth, on the other hand,

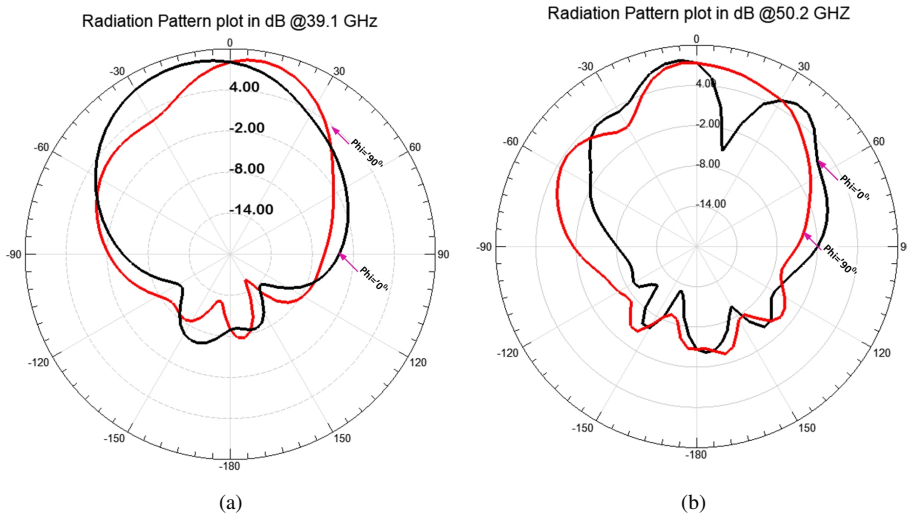


Figure 10. The 2D radiation pattern plot in dB of proposed antenna (a) at 39.1 GHz (b) at 50.2 GHz.

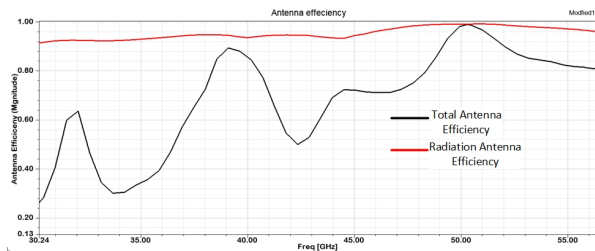


Figure 11. Efficiency of engineered antenna

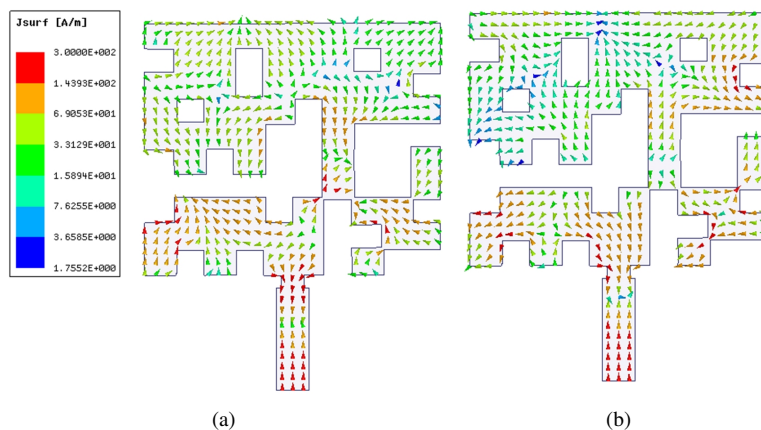


Figure 12. Surface Current distribution of genetically optimized antenna (a) at 39.1 GHz and (b) 50.2 GHz

is investigated as $S_{11} \leq -6\text{dB}$ and the antenna exhibits low gain when compared to this research. Additionally, this work achieves a gain of 7.6 dB, which is 3 dB greater than the maximum gain reported in the literature. The novelty of this paper may be noticed in bandwidth improvement, directivity and gain augmentation from a single antenna

with dualband operating abilities. These results show that the engineered antenna is appropriate for mm-wave cellular communication, and they were achieved using genetic algorithm.



TABLE II. A comparison of this work with previous literature

No.	Paper	Patch size in terms of λ^2	Resonant frequency	Bandwidth in GHz (S11 \leq -10 dB)	Directivities (dB)	Gains (dB)	Methods
1	[3]	0.74 X 0.79	28 GHz 38 GHz	0.3 0.5	6.7 7.9	- -	U-shaped slot
2	[9]	0.56 X 0.56	28 GHz 45 GHz	1.3 1	7.6 7.2	- -	elliptical slot
3	[25]	0.29 X 0.31	14 GHz 17 GHz	1.8 0.6	7.9 7.3	- -	slot optimization
4	[12]	0.93 X 0.93	28 GHz 38 GHz	1 3	- -	4.7 5.13	slot
5	[24]	0.26 x 0.14	28 GHz 60 GHz	0.4 3.1	- -	3.5 4.6	Double Bow-tie
6	This Paper	0.73 X 0.86	39.2 GHz 50.2 GHz	1.6 3.3	7.9 7.4	7.6 7.3	genetic algorithm

5. CONCLUSION

Using a binary-coded genetic algorithm, this article revealed a dualband microstrip antenna optimization for mm-wave mobile applications. The engineered antenna was resonated at 39.1 GHz and 50.2 GHz whereas the reference model was resonated only at 39.0 GHz. To that purpose, a genetically modified microstrip antenna performed admirably in the operating band of interest. The optimized antenna have achieved 1.6 GHz bandwidth and 7.6 dB gain at 39.1 GHz and 3.3 GHz bandwidth, 7.4 dB gain at 50.2 GHz center frequency. This work can also compared with other related works and the proposed reference antenna in mm-wave frequency. The proposed antenna performs brilliantly in terms of bandwidth and other far-field properties, which makes the antenna practical for mm-wave communication.

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